

# TANJONG KATONG GIRLS' SCHOOL PRELIMINARY EXAMINATION SECONDARY FOUR EXPRESS

CANDIDATE NAME				
CLASS	E		INDEX NUMBER	
MATHEMAT	rics			4048/01
Paper 1			3	1 August 2022
Candidates answ	er on the Question Paper			2 hours
READ THESE IN	STRUCTIONS FIRST			
Write in dark blue You may use an l Do not use staple	number and name on all the wo or black pen. HB pencil for any diagrams or g s, paper clips, glue or correction ON ANY BARCODES.	raphs.		
Omission of esser The use of an app If the degree of a	ons. led for any question it must be s ntial working will result in loss o proved scientific calculator is ex accuracy is not specified in the igures. Give answers in degrees	f marks. pected, where appropriate. question, and if the answer	is not exact, give	e the answer to
	your calculator value or 3.142, ι		the answer in te	rms of $\pi$ .
The number of ma The total of the m	arks is given in brackets [ ] at tharks for this paper is 80.	ne end of each question or p	art question.	
			For Exa	miner's use
Setters: Mdm N Markers: Mr Ang	Ng g, Mdm Lim, Mdm Murni, Mdm I	Ng and Mrs Pang		

This document consists of 24 printed pages, including this page.

#### Mathematical Formulae

Compound interest

Total amount = 
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone =  $\pi r l$ 

Surface area of a sphere =  $4 \pi r^2$ 

Volume of a cone = 
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere = 
$$\frac{4}{3}\pi r^3$$

Area of triangle 
$$ABC = \frac{1}{2}ab\sin C$$

Arc length =  $r\theta$ , where  $\theta$  is in radians

Sector area = 
$$\frac{1}{2}r^2\theta$$
, where  $\theta$  is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation = 
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

## Answer all the questions.

1	Write the following numbers in order	er of size	, starting with	the largest.
---	--------------------------------------	------------	-----------------	--------------

$$1\frac{1}{9}, -\frac{22}{7}, \left(\frac{\sqrt{2}}{2}\right)^4, -\pi$$

[1]

2 Simplify  $16(a^{-2}b^4)^{-\frac{3}{4}}$  and leave your answer in positive index form.

3 Show and explain that  $(5n-1)^2 + 4$  is a multiple of 5 for all integers of n.

Answer	
	 [2]

BP~	6	2	5
-----	---	---	---

4	Facto	rice
4	racio	11180

(a) 
$$36y^2 - 25(x-1)^2$$

Answer ......[1]

**(b)** 
$$12x^2 - 2y^2 + 5xy$$

Answer ..... [1]

5 Rearrange the formula to make x the subject.

$$y = \sqrt{\frac{x^2 + 1}{x^2 - 4}} \text{ where } y > 0.$$

Answer ..... [3]

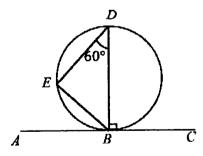
- One solution of the equation  $5x^2 + (k-23)x + k = 0$  is x = 3.
  - (a) Find the value of k.

Answer 
$$k = \dots$$
 [1]

(b) Find the second solution of the equation.

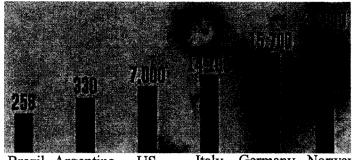
Answer 
$$x = \dots$$
 [2]

Given ABC is a straight line, B, D and E lie on the circumference of the circle,  $\angle DBC = 90^{\circ}$  and  $\angle EDB = 60^{\circ}$ . Find  $\angle DEB$ , giving reason(s) for your answer.



Answer 
$$\angle DEB = \dots$$
 [2]

#### Number of Covid-19 Tests per million people

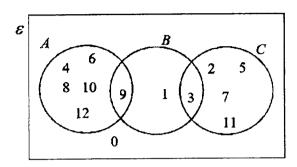


Brazil Argentina US Italy Germany Norway

After this bar graph was shown on Argentinian TV channel C5N, some statisticians claimed that the TV channel was misrepresenting the terrible number of COVID-19 tests in Argentina. Explain which feature of this bar graph is misleading and how it leads to the misrepresentation. Justify your answer with reference to the bar graphs.

Answer	
	[2]

9  $\mathcal{E} = \{\text{non-negative integers}, x: 0 \le x \le 12\}.$ The Venn diagram shows the elements of  $\mathcal{E}$  and the three sets A, B and C. A is the set of composite numbers and C is the set of prime numbers.



(a) Describe the elements of set B.

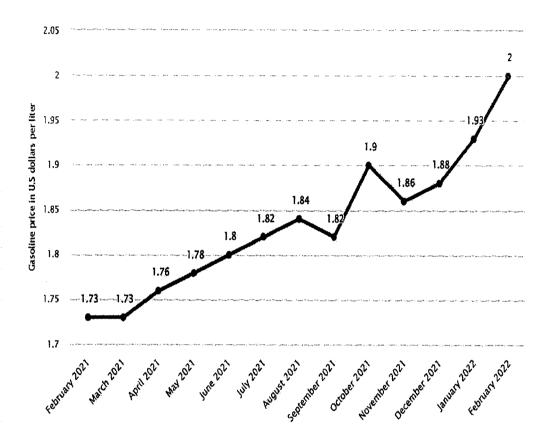
Ansv	wer	[1]
••••	······································	
(b)	List the elements contained in the set $(A \cup B')'$ .	
	Answer $(A \cup B')' = \dots$	[1]

(c) Underline the correct statements from the list below.

$$A' \cap B' \neq \emptyset$$
  $n[(A \cup B)'] = 5$   $\{3\} \subset A \cup B$   $\{9\} \notin A \cap C$  [2]

The line graph shows the average monthly prices of gasoline in Singapore from February 2021 to February 2022 (in U.S. dollars per litre).

#### Average Monthly Prices of Gasoline in Singapore from Feb 2021 to Feb 2022



(a) Find the percentage increase in gasoline price from February 2021 to February 2022.

Answer .....% [1]

(b) Jane claimed that the current gasoline price of US\$2.34 per litre is 30% more expensive than before. Which month and year is she comparing the current gasoline price with?

Answer ..... [1]

(c)	If the gasoline price increases by 1.5% every month starting February 2022,
` '	calculate the gasoline price 1 year later, in February 2023. Give your answer
	rounded to the nearest cent.

Answer US\$...../litre. [2]

11	A The table shows the mass of a fruit, $m$ g, with a diameter of $x$ cm. Determine whether
	m is directly proportional to $x^3$ .

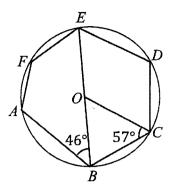
Diameter, x cm	7	8	9	10
Mass, m g	61.74	92.16	131.22	180

Answer	[2]

12 y is inversely proportional to  $\sqrt[3]{x}$ . When y is increased by 10%, calculate the percentage decrease in x.

Answer ......% [2]

13 The diagram shows a circle with centre O. BOE is a straight line. Given that  $\angle ABO = 46^{\circ}$  and  $\angle BCO = 57^{\circ}$ , find, stating your reason(s) clearly,



(a)  $\angle ADE$ 

Answer°	[1]
---------	-----

(b)  $\angle AFE$ 

A	 Γ1
Answer	 [1

(c)  $\angle BEC$ .

Answer ......° [1]

A shop sells Beauty Bath Soap that comes in two geometrically similar bottles of size 125 ml and 1000 ml as shown.



(a) Find the ratio of the height of the smaller bottle to that of the larger bottle in the form 1:n.

Answer	 [1]

(b) At a sales, the price of the bottle with the content of 125 ml and 1000 ml are priced at \$1.90 and \$9.90 respectively. Explain which bottle provides better value for money. Support your answer with calculations.

Answer	[1]

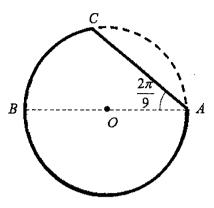
(c) Vouchers and posters were used to advertise this product. The ratio of the lengths of the vouchers to that of the posters were 1: 4. If the size of each voucher is 24.75 cm<sup>2</sup>, find the size of the posters in m<sup>2</sup>, written in standard form.

Answer ......  $m^2$  [2]

15	In an $n$ -sided polygon, the sum of interior angles is $1080^{\circ}$ .				
	(a)	Find the value of $n$ .			
		Answer $n = \dots $ [1]			
	(b)	The interior angles are $x, x + 10^{\circ}, x + 20^{\circ},, [x + (n-1)10^{\circ}]$ . Find the smallest exterior angle.			
		Answer° [2]			

16	Two numbers 528 and 756 written as product of their prime factors are $528 = 2^4 \times 3 \times 11$ $756 = 2^2 \times 3^3 \times 7$ Find					
	(a)	the smallest positive integer x for which 528x is a multiple of 756.				
	(b)	the smallest positive integer $y$ for which $\frac{528}{y}$ is a factor of 756.	[2]			
		Answer	[2]			

17 The figure below shows a major segment of a circle ABC where radius OA = 6 cm and  $\angle OAC = \frac{2\pi}{9}$  radians.



(a) Show that the length of the arc BC is  $\frac{8\pi}{3}$  cm.

[1]

Calculate

(b) the perimeter of the major segment ABC,

7
,

(c) the area of the minor segment that was cut off.

18	Given A is the point $(2, -3)$	and $B$ is the point (5,	$m), \overrightarrow{CD}$	= (	(8)	į
----	--------------------------------	--------------------------	---------------------------	-----	-----	---

(a) Express  $\overrightarrow{AB}$  as a column vector in terms of m.

Answer ......[1]

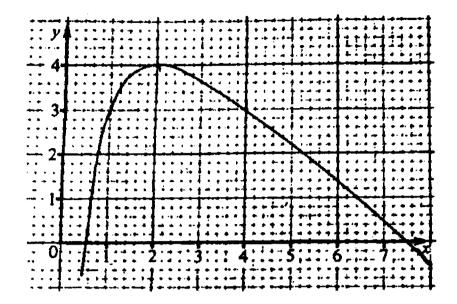
(b) If  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{CD}$ , find the value of m.

 $Answer m = \dots [2]$ 

(c) If  $|\overrightarrow{AB}| = \frac{1}{2} |\overrightarrow{CD}|$ , find  $|\overrightarrow{AB}|$ .

Answer  $|\overrightarrow{AB}|$  = .....units [1]

19 Part of the graph of  $y = 8 - x - \frac{4}{x}$  is drawn on the grid.



Solve each equation below for x in the range 0 < x < 8, by drawing another straight line on the graph. Leave your answer(s) in 1 decimal place.

(a) 
$$x + \frac{4}{x} = 5$$

Answer 
$$x = .....$$
 or ..... [2]

**(b)** 
$$7 - \frac{4}{x} = \frac{x}{2}$$

Answer 
$$x = \dots$$
 [3]

20 The heights, in cm, of 15 boys and 18 girls were recorded in the Back-to-back Stemand-Leaf diagram below.

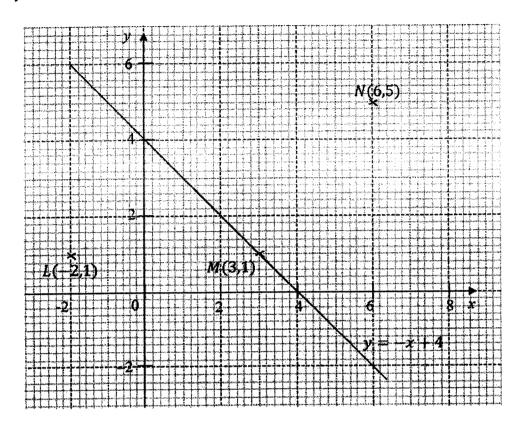
			Boys								Girls	i		
							14	8	8					
						9	15	2	x	x	8	8	9	9
			9	8	б	5	16	v	y	y	z	z		
8	6	5	4	2	1	1	17	2	3	4	5			
				4	2	0	18							
	'	K	ey (Bo	oys)						I	ζey ((	irls)		
		9 15 n	neans	159 c	m					14 8	mean	s 148	cm	

(a) If the median height of the girls is 161 cm, write down the value of y.

Answer 
$$y = \dots$$
 [2]

(b) Find the interquartile range of the boys' heights.

The diagram shows three points L(-2,1), M(3,1) and N(6,5) and the line y = -x + 4.



(a) Calculate the exact value of  $\cos \angle LMN$ .

Answer ..... [2]

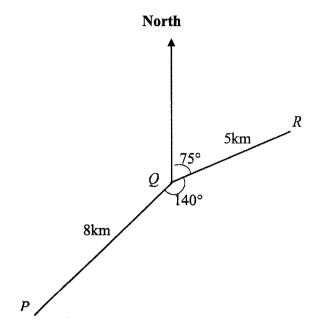
(b) P is the point (3, k) and the area of triangle LMP is 15 square units. Find the possible value(s) of k.

Answer  $k = \dots$  [3]

(c) Given that y = -x + 4 is the line of symmetry of triangle LMQ, write down the coordinates of Q.

Answer Q(.....) [1]

A ship sails 8 km from port P to port Q. It then sails 5 km from port Q to port R on a bearing of 075°.



- (a) Given that  $\angle PQR = 140^{\circ}$ , calculate
  - (i) the bearing of Q from P,

Answer ..... ° [1]

(ii) how far Q is east of P.

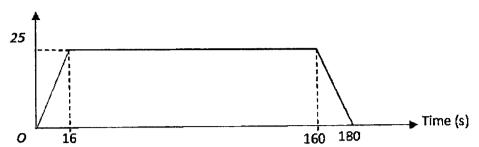
Answer ...... km [2]

(b) An island X is located at a bearing of  $085^{\circ}$  from P and  $160^{\circ}$  from Q.

anjong Kat	ong Gi	irls' School 4048/S4Prelim/01/2022 [Turn o	ver
		Answer minutes	[3]
•	(ii)	If a boat travels from $P$ to $X$ at a speed of 40km/h, calculate the time, in minutes, that the boat takes to reach $X$ .	
		Answer °	[1]
(	(i)	Find $\angle PQX$ .	

23 The diagram shows the speed-time graph of a car as it travelled from point A to B.

Speed (m/s)



(a) Find the speed of the car at 165 seconds.

Answer......m/s [2]

(b) A stationary motorcycle started travelling at the same time as the car, taking the same route in opposite direction from point B to A. Given that the motorcycle travelled at a constant acceleration of 3 m/s<sup>2</sup> and it passed by the car at T seconds where 16 < T < 160, show that

$$1.5T^2 + 25T - 4250 = 0.$$

[3]

### End of Paper

# Sec 4 Prelim Math Paper 2

1	(a)	Exp	ress as a single fraction in its simplest form	•
		(i)	$\frac{24q^2}{63p^3} \div \frac{9q^5}{21p},$	[1]

(ii) 
$$\frac{1}{m-4} + \frac{2m}{m^2-16}$$
. [2]

**(b)** Simplify 
$$\frac{3x-9}{2x-xy+3y-6}$$
. [3]

(c) Solve the equation 
$$(x+2)(x-5) = (x-5)(4x-7)$$
. [3]

2	Bala	019, Alan and Bala decided to start a business together. Alan invested \$210 000 and a invested \$140 000. They agreed that all profit should be divided in the same ratio he sums of the money they invested.	
	(a)	In 2019, the profit was \$20 000. Calculate Alan's share of the profit.	[2]
	(b)	Due to the pandemic, the total profit in 2020 dropped to \$12 500. Calculate the percentage decrease in profit from 2019 to 2020.	[1]
	(c)	To expand their business, they decided to borrow \$100 000 from a bank. The bank charged an interest rate of 2.4% per annum compounded half yearly. Calculate how much interest they need to pay after 5 years. Give your answer correct to the nearest dollars.	[3]

Alan and Bala can choose to import their raw materials which cost RM40 000 in Malaysia or NT\$265 000 in Taiwan. The exchange rate between Singapore and Malaysia is S\$1 = RM\$3.20 and the exchange rate between Taiwan and Singapore is NT\$100 = S\$4.60. There is a freight charge of 2% for the raw materials from Taiwan only. Determine which country they should import their raw materials from.

[4]

[2]

3	A wholesaler supplies snacks and delivers to two stalls. The matrix, S, shows the
	number of each type of snacks per delivery made to Stalls A and B. In a week, the
	wholesaler delivers 5 times to Stall A and 7 times to stall B.

san	dwich	cake	pie	
	(25	20	13	Stall $A$
<b>S</b> =	40	10	21	G. 11 D
	40	18	21)	Stall B

- (a) The wholesaler charges the stalls \$2.00, \$0.70 and \$1.50 each for sandwich, cake and pie respectively. Represent these prices in column matrix **P**. [1]
- (b) Evaluate the matrix C = SP.

- (c) State what each of the elements of C represents. [1]
- (d) The amount collected by the wholesaler in a week from Stall A and Stall B respectively is represented by a  $2 \times 1$  matrix, W. Using only matrix [2] multiplication, find W.

(e) Hence, find the total amount collected by the wholesaler in a week. [1]

4	(a)	These are the first four terms in a sequence.	
		-2 1 4 7	
		Find an expression in terms of n for the nth term of the sequence	Г17

(b) Study the following number pattern of the Pythagorean Triples.

Row	Pythagorean Triples
1	$5^2 = 3^2 + 4^2$
2	$13^2 = 5^2 + 12^2$
3	$25^2 = 7^2 + 24^2$
4	$41^2 = 9^2 + 40^2$
5	$p^2 = q^2 + 60^2$
:	:
N	$P_N^2 = Q_N^2 + R_N^2$

(i) Write down the value of p and of q in Row 5. [2]

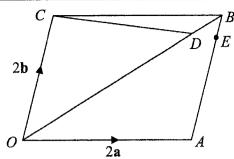
(ii) Write down the Pythagorean Triples in Row 10 when  $P_{10} = 221$ . [1]

(iii) When  $Q_N = 111$ , find N. [2]

	<u>, , , , , , , , , , , , , , , , , , , </u>	
(iv)	Given that $R_N = aN^2 + bN$ , find the value of a and of b.	[4]

(v) Explain with reason why it is not possible for 2021 to be a number of  $R_N$ . [2]

5 (a)



The diagram shows a parallelogram OABC. The point D on OB is such that OD = 5DB. The point E on AB is such that AB : EB = 5:1. Given that  $\overrightarrow{OA} = 2\mathbf{a}$  and  $\overrightarrow{OC} = 2\mathbf{b}$ .

(i)	Express in terms of a and b, giving each of your answers in its simplest	
	form.	
	(a) $\overrightarrow{OB}$ ,	[1]

$$| \textbf{(b)} | \overrightarrow{CD}.$$
 [2]

(ii) Show that C, D and E are collinear.

[3]

(iii)	Find the numerical value of	Area of ΔODC	
(111)	ring the numerical value of	Area of parallelogram <i>QABC</i>	[1]

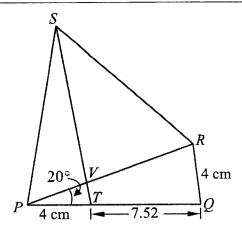
(b) It is given that  $\overrightarrow{PQ} = \begin{pmatrix} 5 \\ 1 \end{pmatrix}$  and the coordinates of R are (4,0). Find the coordinates of the point S such that PQRS is a parallelogram.

- An aircraft flew from Town A to Town B and made a return trip to Town A from Town B. The total distance covered was 1200 km. The speed of the aircraft in still air is 200 km/h. The aircraft flew against the wind when flying from Town A to Town B, and flew wind assisted when flying back to Town A from Town B.
  - (a) The speed of the wind, which is constant throughout, is x km/h. The time taken by the aircraft, in hours, to fly from Town A to Town B is  $\frac{600}{200-x}$ . Write down an expression, in terms of x, the time taken by the aircraft, in hours, to fly from Town B to Town A.
  - (b) The time taken to fly against the wind is 10 minutes longer than when it took to fly wind assisted. Write down an equation in terms of x and show that it reduces to  $x^2 + 7200x 40\ 000 = 0$ .

(c) Showing your working clearly, solve the equation  $x^2 + 7200x - 40\,000 = 0$ , giving your solutions correct to 2 significant figures. [4]

(d) Find the time taken for the whole trip.

7



 $\triangle PQR$  is an isosceles triangle with  $\angle QPR = 20^{\circ}$ . S is a point outside  $\triangle PQR$  such that  $\triangle PRS$  is an equilateral triangle and SVT is a straight line that meets PR and PQ at V and T respectively. It is given that QR = TP = 4 cm and TQ = 7.52 cm.

(a) Show that  $\triangle PQR$  is congruent to  $\triangle STP$ . Give a reason for each statement you make.

[3]

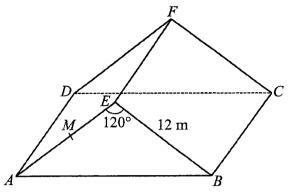
**(b)** Show that  $\triangle STR$  is an isosceles triangle.

[2]

(c) Find  $\angle STR$ .

[2]

A roof in the shape of a triangular right prism is constructed as shown below such that ABCD is a rectangle, ADFE and BCFE are squares. AE = BE = 12 m,  $\angle AEB = 120^{\circ}$  and M is the midpoint of AE.



Find

(a) the area of triangle ABE,

[2]

(b)  $AB^2$ ,

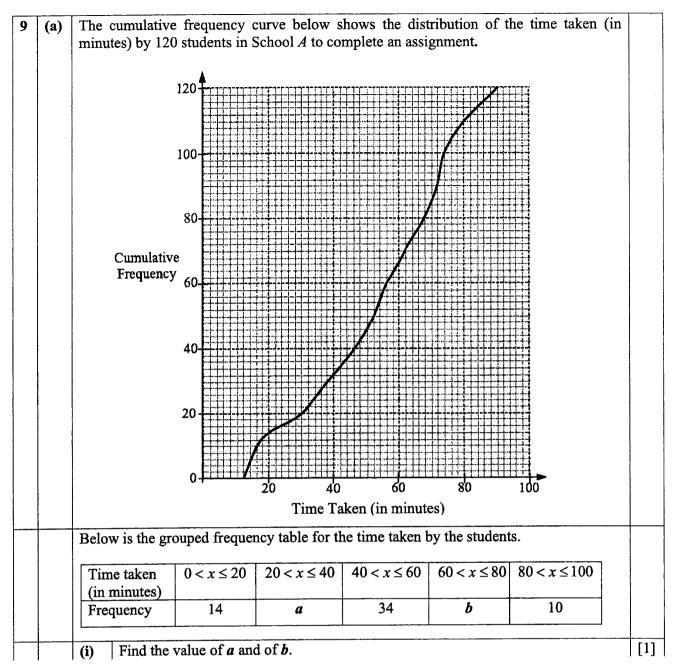
[2]

(c) AC,

[2]

**(d)** ∠*AEC*,

[3]



-	(ii) Estimate the mean time taken by the students.	[1]

(iii) Estimate the standard deviation of the time taken by the students.

[1]

(iv) 120 students from School B completed the same assignment, and the analysis of their time taken is represented in the table below.

Mean time taken	60
Standard deviation	13.6

Make two comments comparing the time taken by the students from the 2 schools.

(b) Ali, Bryan and Chandra took part in a game of dart throwing. The probabilities that Ali, Bryan and Chandra will hit the target in a single throw are  $\frac{1}{6}$ ,  $\frac{1}{5}$  and  $\frac{1}{4}$  respectively.

- (i) For the first game, all three of them throw the dart at the target at the same time. Find the probability that all of them hit the target. [2]
- (ii) In the second game, they each make a single throw of the dart at the target in the order of Ali, Bryan and Chandra. For this game, once the target is hit, the game will end. Find the probability the target is hit.

[3]

Daryl owns a concert hall with a full capacity of 120 seats. He conducted a survey to find out how much to charge for tickets. The detail of the survey is below:

Price of one ticket	Number of people who will attend the concert
\$6.00	120
\$7.50	110
\$9.00	100
\$10.50	90
:	:

		<u> </u>	
 (a)	Write	down the revenue he will get if all 120 seats are sold.	[1]
(b)		I noticed that for every \$1.50 increase in the price of one ticket, the number of le who attend the concert drops by 10.	
	(i)	Find the revenue if he makes three \$1.50 increases to the price from \$6.	[1]
	(ii)	Let <i>n</i> be the number of \$1.50 increase in the price of the tickets, explain why the revenue $R$ , in dollars is given by $720 + 120n - 15n^2$ .	[3]
		2000 200 200 200 200 200 200 200 200 20	
	(iii)	Explain why the number of \$1.50 increase in price should be less than 12.	[1]
 	(iv)	By drawing a suitable graph for $n < 12$ on the grid opposite, work out how much should Daryl charge his ticket to maximum revenue.	[4]
		•	

## TANJONG KATUNG

BP~665

1	$1\frac{1}{9}, \left(\frac{\sqrt{2}}{3}\right)^4, -\pi, -\frac{22}{7}$	-	
	$\left(\frac{1}{9}, \left(\frac{\pi}{2}\right), -\pi, -\frac{\pi}{7}\right)$		
2	T 3		
2	$16a^{\frac{3}{2}}$		
	$b^3$		
3	$5(5n^2-2n+1)$ is a multiple of 5	for all integ	ers of n
4(a)	(6y+5x-5)(6y-5x+5)	4(b)	(4x-y)(3x+2y)
-()	(Oy   3x 3)(Oy 3x   0)		(1x y)(0x , 2y)
5	$4x^2 \pm 1$		
	$x = \pm \sqrt{\frac{4y^2 + 1}{y^2 - 1}}$		
	$\sqrt{y^2-1}$		
6(0)	1.	6(h)	2
6(a)	k=6	6(b)	The other solution is $x = \frac{2}{5}$
7	Angle <i>DEB</i> = 90°		
		^.1 1	1 1 1 0
8	Misleading feature: The heights of	the bars are	not proportional to the number of
	covid-19 tests per million people.		
	I Effect of misleading feature. The h	heights of the	- l
	1	-	e bars suggest that Argentina tests abour
	1	-	as the *USA. However, Argentina tests about
	three-quarter the number of people	e per million	as the *USA. However, Argentina test
	three-quarter the number of people 330 people per million while the U	e per million	
	three-quarter the number of people 330 people per million while the U times.	e per million JSA tests 70	as the *USA. However, Argentina test 00 people per million, which is about 2
	three-quarter the number of people 330 people per million while the U times.  *Accept correct comparison with or	e per million JSA tests 70 other countri	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. 4/5 vs 43 times,
	three-quarter the number of people 330 people per million while the U times.	e per million JSA tests 70 other countri	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. 4/5 vs 43 times,
9(a)	three-quarter the number of people 330 people per million while the U times.  *Accept correct comparison with a Germany 2/3 vs 48 times or Norwall	e per million USA tests 70 other countri ay ½ vs 68 t	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. 4/5 vs 43 times, imes)
	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9.	e per million JSA tests 70 other countri ay ½ vs 68 t	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes) $(A \cup B')' = A' \cap B = \{1, 3\}$
	three-quarter the number of people 330 people per million while the U times.  *Accept correct comparison with a Germany 2/3 vs 48 times or Norwall	e per million JSA tests 70 other countri ay ½ vs 68 t	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes) $(A \cup B')' = A' \cap B = \{1, 3\}$
9(c)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9.	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs 43 times, imes) $(A \cup B')' = A' \cap B = \{1,3\}$ $\{9\} \notin A \cap C$
9(c) 10(a)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9.  A' \cap B' \neq \varphi n[(A \cup B)'] = 5 \{3\)	e per million JSA tests 70 other countri ay ½ vs 68 t	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes) $(A \cup B')' = A' \cap B = \{1, 3\}$
9(c) 10(a)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9.  A' ∩ B' ≠ Ø n[(A ∪ B)'] = 5 {3}  15.6%  US\$2.39	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes) $A \cup B' = A' \cap B = \{1, 3\}$ $\{9\} \notin A \cap C$ June 2021
9(c) 10(a) 10(c)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9.  A' ∩ B' ≠ Ø n[(A ∪ B)'] = 5 {3}  15.6%  US\$2.39	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs 43 times, imes) $(A \cup B')' = A' \cap B = \{1,3\}$ $\{9\} \notin A \cap C$
9(c) 10(a) 10(c)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9.  A' ∩ B' ≠ Ø n[(A ∪ B)'] = 5 {3}  15.6%  US\$2.39	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes) $A \cup B' = A' \cap B = \{1, 3\}$ $\{9\} \notin A \cap C$ June 2021
9(c) 10(a) 10(c)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9.  A' ∩ B' ≠ Ø n[(A ∪ B)'] = 5 {3}  15.6%  US\$2.39	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes) $A \cup B' = A' \cap B = \{1, 3\}$ $\{9\} \notin A \cap C$ June 2021
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9(c) 10(a) 10(c) 11 12 13(a) 13(c)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9. $A' \cap B' \neq \emptyset  n[(A \cup B)'] = 5$ {3  15.6%  US\$2.39  Since $\frac{m}{x^3} = k$ , where $k$ =0.18 is a normal 24.9%  46°  33°	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 to $ \begin{array}{c c} 9(b) \\ \hline 3\} \subseteq A \cup B \\ \hline \end{array} $ $ \begin{array}{c c} 10(b) \\ \hline \end{array} $ $ \begin{array}{c c} 13(b) \\ \end{array} $	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes)
9(a) 9(c) 10(a) 10(c) 11 12 13(a) 13(c) 14(a)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwald Elements of set B are factors of 9. $A' \cap B' \neq \emptyset  n[(A \cup B)'] = 5  \{3\}$ 15.6%  US\$2.39  Since $\frac{m}{x^3} = k$ , where $k=0.18$ is a normal 24.9%  46°  33°	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$ on-zero cons $13(b)$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs 43 times, imes) $(A \cup B')' = A' \cap B = \{1, 3\}$ $\{9\} \notin A \cap C$ June 2021 $\text{tant, } m \text{ is directly proportional to } x^3.$
9(c) 10(a) 10(c) 11 12 13(a) 13(c)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with a Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9. $A' \cap B' \neq \emptyset  n[(A \cup B)'] = 5  \{3\}$ $15.6\%$ $US$2.39$ $Since \frac{m}{x^3} = k, \text{ where } k=0.18 \text{ is a notation of } k=0.$	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$ on-zero cons $13(b)$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs $43$ times, imes)
9(c) 10(a) 10(c) 11 12 13(a) 13(c) 14(a)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwall Elements of set B are factors of 9. $A' \cap B' \neq \emptyset  n[(A \cup B)'] = 5  \{3\}$ 15.6%  US\$2.39  Since $\frac{m}{x^3} = k$ , where $k=0.18$ is a normal 24.9%  46°  33°  1:2  1000ml bottle cost \$0.0053 less per better value for money.	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$ on-zero cons $13(b)$	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs 43 times, imes) $(A \cup B')' = A' \cap B = \{1, 3\}$ $\{9\} \notin A \cap C$ June 2021 $\text{tant, } m \text{ is directly proportional to } x^3.$
9(c) 10(a) 10(c) 11 12 13(a) 13(c) 14(a)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwald Elements of set B are factors of 9. $A' \cap B' \neq \emptyset  n[(A \cup B)'] = 5  \{3\}$ 15.6%  US\$2.39  Since $\frac{m}{x^3} = k$ , where $k=0.18$ is a normal 24.9%  46°  33°  1:2  1000ml bottle cost \$0.0053 less per better value for money.  OR	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$ $13(b)$ $14(c)$ er ml than 12	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs 43 times, imes) $(A \cup B')' = A' \cap B = \{1, 3\}$ $\{9\} \notin A \cap C$ June 2021  tant, $m$ is directly proportional to $x^3$ .
9(c) 10(a) 10(c) 11 12 13(a) 13(c) 14(a)	three-quarter the number of people 330 people per million while the Utimes.  *Accept correct comparison with Germany 2/3 vs 48 times or Norwald Elements of set B are factors of 9. $A' \cap B' \neq \emptyset  n[(A \cup B)'] = 5  \{3\}$ 15.6%  US\$2.39  Since $\frac{m}{x^3} = k$ , where $k=0.18$ is a normal 24.9%  46°  33°  1:2  1000ml bottle cost \$0.0053 less per better value for money.  OR	e per million USA tests 70 other countri ay $\frac{1}{2}$ vs 68 t $9(b)$ $3\} \subseteq A \cup B$ $10(b)$ $13(b)$ $14(c)$ er ml than 12	as the *USA. However, Argentina test 00 people per million, which is about 2 es (Italy approx. $4/5$ vs 43 times, imes) $(A \cup B')' = A' \cap B = \{1, 3\}$ $\{9\} \notin A \cap C$ June 2021 $\text{tant, } m \text{ is directly proportional to } x^3.$

15(a)	n = 8	15(b)	10°
16(a)	smallest positive integer $x = 63$	16(b)	smallest positive integer $y = 44$
17(b)	36.4 cm	17(c)	13.7 cm <sup>2</sup>
18(a)	(3)	18(b)	$m = -\frac{3}{4}$
	$\binom{3}{m+3}$		$m = \frac{4}{4}$
18(c)	5 units		
10()	10 (0)	10(6)	
19(a)	x = 1.0  or  4.0  (accept  3.9)	19(b)	x = 0.6
20(a)	y = 3	20(b)	IQR of boy's height = $178 - 168 =$
20(4)	y = 3		10 cm
21(a)	3	21(b)	k = 7  or  -5
	$\cos \angle LMN = -\frac{3}{5}$		
21(c)	Q(3,6)		
22()(2)		22(2)(32)	A #01
22(a)(i)	035°	22(a)(ii)	4.59km
22(b)(i)	55°	22(b)(ii)	10.2 min
23(a)	Speed = 18.75 m/s		

## Sec 4 Prelim Math Paper 2 Solutions

1 (a) Express as a single fraction in	its simplest form	
(i) $\frac{24q^2}{63p^3} \div \frac{9q^5}{21p}$ ,		[1]
Solutions	Skills/Concept	
$=\frac{24q^2}{63p^3}\times\frac{21p}{9q^5}$	Take reciprocal: $\frac{24q^2}{63p^3} \times \frac{21p}{9q^5}$	
$=\frac{8}{9p^2q^3}$	Laws of indices: $a^{m+n} = a^m \times a^n$ $a^{m-n} = a^m \div a^n$	
(ii) $\frac{1}{m-4} + \frac{2m}{m^2-16}$ .		[2]
Solutions	Skills/Concept	
$= \frac{1}{m-4} + \frac{2m}{(m-4)(m+4)}$	Quadratic Identity: $a^2 - b^2 = (a + b)(a - b)$	
$=\frac{(m+4)+2m}{(m-4)(m+4)}$	Express as single fraction	
$=\frac{3m+4}{(m-4)(m+4)}$		
(m-4)(m+4)		
<b>(b)</b> Simplify $\frac{3x-9}{2x-xy+3y-6}$ .		[3]
Solutions/Alternative Methods	Skills/Concept	
Solutions/Alternative Methods $= \frac{3x-9}{(2x-xy)+(3y-6)} = \frac{3x-3}{x(2-y)+3}$	$\frac{-9}{3(y-2)}$ Factorisation by grouping	
$=\frac{3(x-y)}{x(2-y)}$	$\frac{-3)}{3(2-y)}$ Change of sign	
	$-\frac{3}{y-2}$ also acceptable	
$=\frac{3}{2-y}$		
(c) Solve the equation $(x+2)(x+2)$	(x-5) = (x-5)(4x-7).	[3]
Solutions/Alternative Methods	Skills/Concept	
(x+2)(x-5) - (4x-7)(x-5) = 0 $(x-5)[(x+2) - (4x-7)] = 0$ $(x-5)(9-3x) = 0$	Factorisation of quadratic function  Solving quadratic equation	
(x-3)(9-3x) = 0 x=3 or $x=5$		

•	T- 2010 Al I D-1- I II- I		an invested \$210,000 and			
2	In 2019, Alan and Bala decided to start a business together. Alan invested \$210 000 and					
	Bala invested \$140 000. They agreed that all profit should be divided in the same ratio as the sums of the money they invested.					
Salv		Skills/Concept	of the profit.	[2]		
Som						
	Alan's share of profit = $\frac{3}{5} \times 20~000$	Ratio: $\frac{21000}{210000+1}$	<del>10000</del> = <del>5</del>			
	3	210000 + 1	40000 5			
	= \$12 000	:4 in 2020 duamed	to \$12 500 Calculate the	]		
	(b) Due to the pandemic, the total prof		to \$12 500. Calculate the	Γ1 <b>7</b>		
Call	percentage decrease in profit from 2 ations/Alternative Methods	Skills/Concept				
Solu		Skins/Concept	difference			
	percentage decrease in profit	Percentage decrea	$se = \frac{difference}{original} \times 100$			
	$= \frac{20\ 000 - 12\ 500}{20\ 000} \times 100\%$		original			
	20 000					
	= 37.5%			4		
	(c) To expand their business, they decide					
	charged an interest rate of 2.4% per		* *			
	how much interest they need to pay	after 5 years. Give	your answer correct to the			
	nearest dollars.			[3]		
Solu	tions/Alternative Methods	Skills	/Concept			
	$\left[ \left( 2.4 \right) \right]^{5\times2}$	_				
	Interest = $100\ 000 \left[ 1 + \frac{\left( \frac{2.4}{2} \right)}{100} \right]^{32} - 100\ 000$	n=5	×2			
	Interest = $100\ 000   1 + \frac{100}{100}   -100\ 000$	00				
	100	r=2	$4 \div 2$			
	010 ((0.1770					
	= \$12 669.1778					
	= \$12 669	<del></del>	d up to nearest dollars	1		
	(d) Alan and Bala can choose to import					
	Malaysia or NT\$265 000 in Taiwar					
	Malaysia is $S$1 = RM$3.20$ and the					
	is $NT$100 = S$4.60$ . There is a frei			1		
	Taiwan only. Determine which cou	intry they should in	mport their raw materials			
	from.		G1 *** /G	[4]		
Solu	utions/Alternative Methods	40.000	Skills/Concept			
	Amount paid in S\$ for Malaysia import =	40 000	Exchange rate for			
		3.2	Malaysia Ringgit			
	= \$	\$12 500				
	Amount paid in S\$ for Taiwan import =	$102(265\ 000)$	Exchange rate for Tai			
	Amount paid in 55 for Taiwan import	$\frac{100}{100} \left( \frac{100}{100} \right)^{4.0}$	dallars	lwan		
		\$12 433.80	dollars			
	_	Ψ122 TJJ,UU	Include 20/ fresht -1			
			Include 2% freight ch	iarge		
	They should import their raw materials	from Taisvan bacc	ICA Compara with differen	mea		
	the total amount paid is <u>\$\$66.20</u> lower co			HUU		
l	inc was amount para is source tower co	inparcu w maiaysi	a.   III values			

3	A wholesaler supplies snacks and delivers to two stalls. The matrix, S, shows the				
	number of each type of snacks per delivery made to Stalls A and B. In a week, the wholesaler delivers 5 times to Stall A and 7 times to stall B.				
	wholesaler derivers 5 times to Stan A and 7 times to st	an b.			
	sandwich cake pie				
	$\begin{pmatrix} 25 & 20 & 13 \end{pmatrix} S$	Itall A			
	$\mathbf{S} = \begin{pmatrix} 25 & 20 & 13 \\ & & \\ 40 & 18 & 21 \end{pmatrix} \mathbf{S}$				
	(40 18 21 <i>)</i> S	tall B			
	(a) The wholesaler charges the stalls \$2.00, \$0.70 are and pie respectively. Represent these prices in co				
Solu	and pie respectively. Represent these prices in ecutions/Alternative Methods	Skills/Concept			
	(2.00)				
	$\mathbf{P} = \begin{vmatrix} 0.70 \end{vmatrix}$	Column matrices 3×1			
	$\begin{pmatrix} 1.50 \end{pmatrix}$				
	(b) Evaluate the matrix C = SP.	[2]			
Solu	tions/Alternative Methods	Skills/Concept			
	$\mathbf{C} = \begin{pmatrix} 25 & 20 & 13 \\ 40 & 18 & 21 \end{pmatrix} \begin{pmatrix} 2.00 \\ 0.70 \\ 1.50 \end{pmatrix}$ $= \begin{pmatrix} 83.50 \\ 124.10 \end{pmatrix}$	Multiplying matrices, Order: $(2\times3)\times(3\times1)=(2\times1)$			
	(83.50)				
	= (124.10)				
	(c) State what each of the elements of C represents.	[1]			
Solu	The elements represent the amount collected by the	Skills/Concept			
	wholesaler from the sales of snacks per delivery from Stall A and Stall B respectively.				
	(d) The amount collected by the wholesaler in a respectively is represented by a 2×1 mat				
	multiplication, find W.	Skills/Concept			
Solt	tions/Alternative Methods (5 0) (83 50 0 ) (5)	Matrix multiplication of 2×2 with			
	$\mathbf{W} = \begin{pmatrix} 5 & 0 \\ 0 & 7 \end{pmatrix} \begin{pmatrix} 83.50 \\ 124.10 \end{pmatrix} \text{ or } = \begin{pmatrix} 83.50 & 0 \\ 0 & 124.10 \end{pmatrix} \begin{pmatrix} 5 \\ 7 \end{pmatrix}$	$2\times1$ to get $2\times1$			
	$= \binom{417.50}{868.7}$				
	= (868.7)				
	$=$ $\begin{pmatrix} 417.50\\ 868.7 \end{pmatrix}$				
	(e) Hence, find the total amount collected by the wh				
Solu	ntions/Alternative Methods	Skills/Concept			
	<b>Total amount</b> = $(1 \ 1) \binom{417.50}{868.7}$	Unit matrix (1 1)			
	The total amount collected in a week is \$1286.20				

4	(a)	Thes	e are the fir	st four terms in a s	equence.	· , · · · · ·		
				-2 1	4 7			
	-	Find	an express	ion, in terms of $n$ , f	for the nth	term	of the sequence.	[1]
Sol	utions		native Me				ills/Concept	
•	3(n	-1)-2	2 = 3n - 3 -	2		Ger	neral term: $a + (n-1)d$	
			=3n-5				1st term,	
						<i>d</i> :	constant difference between ter	ms
	(b)	Study	y the follov	ving number patter	n of the Py	ythag	gorean Triples.	
				Row	Pyth	agor	rean Triples	
				1		$5^2 =$	$3^2 + 4^2$	
				2	1	$3^2 =$	$5^2 + 12^2$	
				3	2	$25^2 =$	$7^2 + 24^2$	
				4	4	11 <sup>2</sup> =	$9^2 + 40^2$	
				5		$p^2 =$	$=q^2+60^2$	
				N	$P_{i}$	$\frac{\mathbf{Q}^2}{\mathbf{Q}^2} = \mathbf{Q}^2$	$Q_{N}^{2}+R_{N}^{2}$	
	_	(i)	Write dox	vn the value of $p$ ar	nd of a in	Row	5	[2]
Sol	lutions		native Me		ild Ol q III .	ICOW	Skills/Concept	1[2]
~ 0.	p =						Number patterns	
	q =	11				}		
		(ii)	Write dov	vn the Pythagorean	Triples in	ı Rov	w 10 when $P_{10} = 221$ .	[1]
Sol	lution	s/Alter	native Me				Skills/Concept	
	221	$^{2} = 21^{2}$	$+220^{2}$				Include $P, Q \& R$	
		(iii)	When $Q_N$	= 111, find <i>N</i> .				[2]
So	Solutions/Alternative Methods Skil				Skills/Concept			
	$Q_{\scriptscriptstyle N}$	=2(N	-1) + 3				Find number pattern for $Q_{N}$	
	- 1	= 2 <i>N</i> +						
	1	+1=1					Equate 2N + 1 to 111	
		2N=1						
		N=5	5					

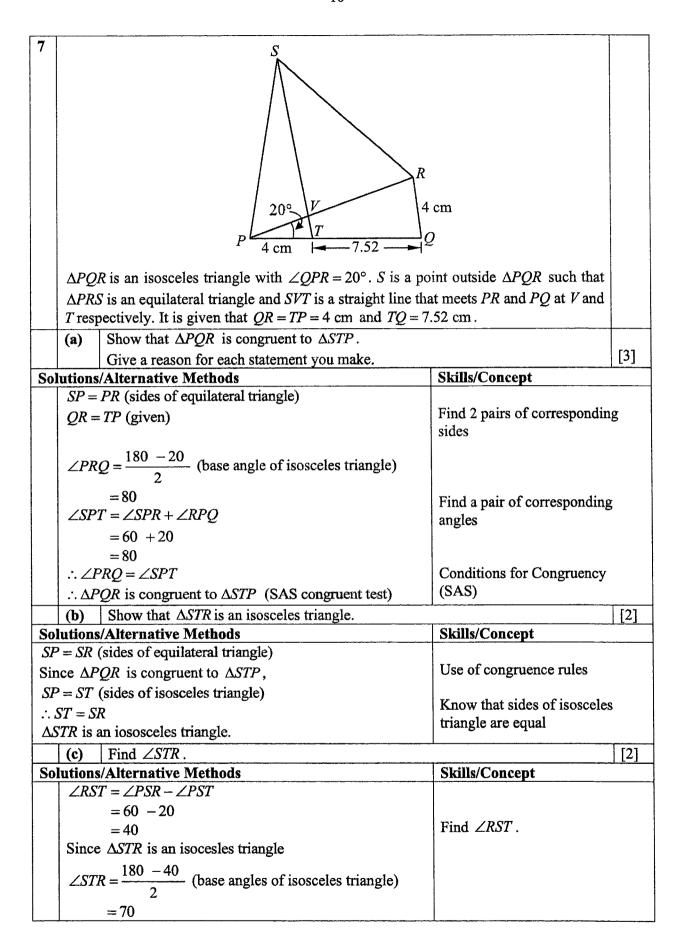
	(iv)	Given that $R_N = aN^2 + bN$ , find the value	of $a$ and of $b$ .	[4]
Solu	tions/Alter	native Methods	Skills/Concept	
	$R_{N} = aN^{2}$	+bN		
	When $N = a(1)^2 + b(1)$ a+b=4	) = 4	Form 1 <sup>st</sup> equation	
	When $N = a(2)^2 + b(2)^2 + b$	a = 2, a = 2 into (1),	Form $2^{nd}$ equation  Solve simultaneous equations  Both $a \& b$ must be correct	
	b=2			·,
	(v)	Explain with reason why it is not possible	for 2021 to be a number of $R_N$ .	[2]
Solu	tions/Alter	native Methods	Skills/Concept	
	$2N^2 + 2N$	$=2(N^2+1)$	Make $R_{_{N}}$ a multiple of 2	
		$n^2 + 2N = 2(N^2 + 1)$ is always even for all $N$ , it is not possible for 2021 which is odd to er of $R_N$ .	Multiples of 2 are even numbers	5

5	(a)	The diagram shows a parallelogram $OABC$ . The point $D$ on $OB$ is such that $OD = 5DB$ . The point $E$ on $AB$ is such that $AB : EB = 5:1$ . Given that $OA = 2a$				
		and $OC = 2\mathbf{b}$ .  (i) Express in terms of <b>a</b> and <b>b</b> , giving each	of your answers in its simplest			
		form.		[1]		
-	1.	1 2,	Chille/Concept	1 -3		
Sol	1	s/Alternative Methods	Skills/Concept			
		$= OA + AB$ $= 2\mathbf{a} + 2\mathbf{b}$	Triangle Law of Vector Addition	n		
		(b) CD.		[2]		
Sol	utions	s/Alternative Methods	Skills/Concept	<u> </u>		
501	T	t = CO + OD				
		$=CO + OD$ $=CO + \frac{5}{6}OB$	Vector addition with $OD = \frac{5}{6}O$	В		
		$= CO + \frac{5}{6}OB$ $= -2\mathbf{b} + \frac{5}{6}(2\mathbf{a} + 2\mathbf{b})$ $= -2\mathbf{b} + \frac{5}{3}\mathbf{a} + \frac{5}{3}\mathbf{b}$ $= \frac{5}{3}\mathbf{a} - \frac{1}{3}\mathbf{b}$				
		(ii) Show that $C$ , $D$ and $E$ are collinear.		[3]		
Sol	ution	s/Alternative Methods	Skills/Concept			
	CE	C = CB + BE	Find CE using vector addition			
		$=2\mathbf{a}+\frac{1}{5}BA$	Make CD a scalar multiple of (	CE		
		$= 2\mathbf{a} + \frac{1}{5}(-2\mathbf{b})$ $= 2\mathbf{a} - \frac{2}{5}\mathbf{b}$	Or any other scalar multiple $DE = \frac{1}{3}\mathbf{a} + \frac{1}{15}\mathbf{b}$			
	CL	$0 = \frac{1}{3}(5\mathbf{a} - \mathbf{b})$ $0 = \frac{2}{5}(5\mathbf{a} - \mathbf{b})$	$= \frac{1}{15}(5\mathbf{a} - \mathbf{b})$ $= \frac{1}{5 \times 3}(5\mathbf{a} - \mathbf{b})$			
	:. C	$CD = \frac{5}{6}CE$	$DE = \frac{1}{5}CD$ Conditions for collinearity			
		ce $CD$ is a scalar multiple of $CE$ and $C$ is a numon point, $C$ , $D$ and $E$ are collinear.	Conditions for collinearity			

(iii)	(iii) Find the numerical value of $\frac{\text{Area of } \triangle ODC}{\text{Area of } \triangle ODC}$		
(111)	Ai	rea of parallelogram <i>OABC</i>	[1]
Solutions/Alter	rnative Methods	Skills/Concept	******
	$\frac{ODC}{OBC} = \frac{\frac{1}{2} \times 5 \times h}{\frac{1}{2} \times 6 \times h}$ $= \frac{5}{6}$ $\frac{\text{ea of } \Delta ODC}{\text{arallelogram } OABC} = \frac{5}{6} \times \frac{1}{2}$ $= \frac{5}{12}$	Use of Area of triangle = $\frac{1}{2}$ × base × height find ratio of 2 triangles with common height.  Or use counting method	
	s given that $PQ = \begin{pmatrix} 5 \\ 1 \end{pmatrix}$ and the redinates of the point S such that I	e coordinates of $R$ are $(4,0)$ . Find the $PQRS$ is a parallelogram.	[2]
Solutions/Alter	native Methods	Skills/Concept	
Let the co	ordinates of $S$ be $(a, b)$		
PQ = SR		PQ = SR for equal vectors in parallelogram	m
$PQ = OR$ $\binom{5}{1} = \binom{4}{0}$ $\binom{a}{b} = \binom{4}{0}$ $= \binom{-1}{-1}$	$-\binom{a}{b}$	R S/Q Clockwise or anti-clockwise for PQRS	
S(-1, -1)	-1)	Must be coordinates	

6	An aircraft flew from Town A to Town B and made a return trip to Town A from Town						
	B. The total distance covered was 1200 km. The speed of the aircraft in still air is 200						
	km/h. The aircraft flew against the wind when flying from Town A to Town B, and						
	flew wind assisted when flying back to Town A from Town B.						
	(a)	(a) The speed of the wind, which is constant throughout, is x km/h. The time taken					
		by the aircraft, in hours, to fly from Town	A to Town B is $\frac{600}{200-x}$ . Write down				
		an expression, in terms of $x$ , the time taker	n by the aircraft, in hours, to fly from [1]				
		Town B to Town A.					
Sol		s/Alternative Methods	Skills/Concept				
	6	00					
	200	) + x					
	(b)	The time taken to fly against the wind is 10 fly wind assisted. Write down an equation to $x^2 + 7200x - 40000 = 0$ .	-				
Sal	ution	us/Alternative Methods	Skills/Concept				
50.		$\frac{00}{00} - \frac{600}{00} = \frac{10}{00}$					
		$\frac{300}{1-x} - \frac{300}{200+x} = \frac{10}{60}$	Forming quadratic equations				
	600	$0.200 \pm x = 600(200 \pm x) = 1$					
		$\frac{0(200+x)-600(200-x)}{(200^2-x^2)} = \frac{1}{6}$	$(200+x)(200-x)=(200^2-x^2)$				
	Į.		as denominator				
	600	$0(200+x)-600(200-x)=\frac{1}{6}(200^2-x^2)$					
	120	$0x = \frac{1}{6}(200^2 - x^2)$					
		$00x = 200^2 - x^2$ + 7200x - 40 000 = 0 (shown)	Simplify equation to required one				
	(c)	Showing your working clearly, solve the ed	$\frac{1}{\text{mustion } x^2 + 7200x - 40000 = 0, \text{ giving}}$				
		your solutions correct to 2 significant figure					
Sol	ution	ns/Alternative Methods	Skills/Concept				
	x2 -	$+7200x - 40\ 000 = 0$	Solving of quadratic equation using				
	"		formula or completing square only				
:	x =	$\frac{-7200 \pm \sqrt{7200^2 - 4(1)(-40000)}}{2(1)}$					
	_	2(1)					
		.55113  or  = -7205.55113	Leave answers in 2 sig fig				
	<u> </u>	.6  or  = -7200  (2 s.f.)					
50		ns/Alternative Methods					
	1	$+7200x - 40\ 000 = 0$	Solve by completing the square				
	1	$+3600)^2 - (3600)^2 - 40\ 000 = 0$	Solve by completing the square				
	1 `	+3600) <sup>2</sup> =13000000					
	1	$=-3600 \pm \sqrt{13000000}$					
	1	.55113  or  = -7205.55113					
	= 5	6.6  or  = -7200  (2 s.f.)	Leave answers in 2 sig fig				
	(d)	Find the time taken for the whole trip.	[2]				
So	lutio	ns/Alternative Methods	Skills/Concept				
	Ti	600 10					
	1111	ne taken = $2 \times \frac{300}{200 + 5.55113} + \frac{10}{60}$	Use $x = 5.55113$ to find time taken to the				
	1	= 6.0046	nearest hour				
		= 6 hours					
So	lutio	ns/Alternative Methods					

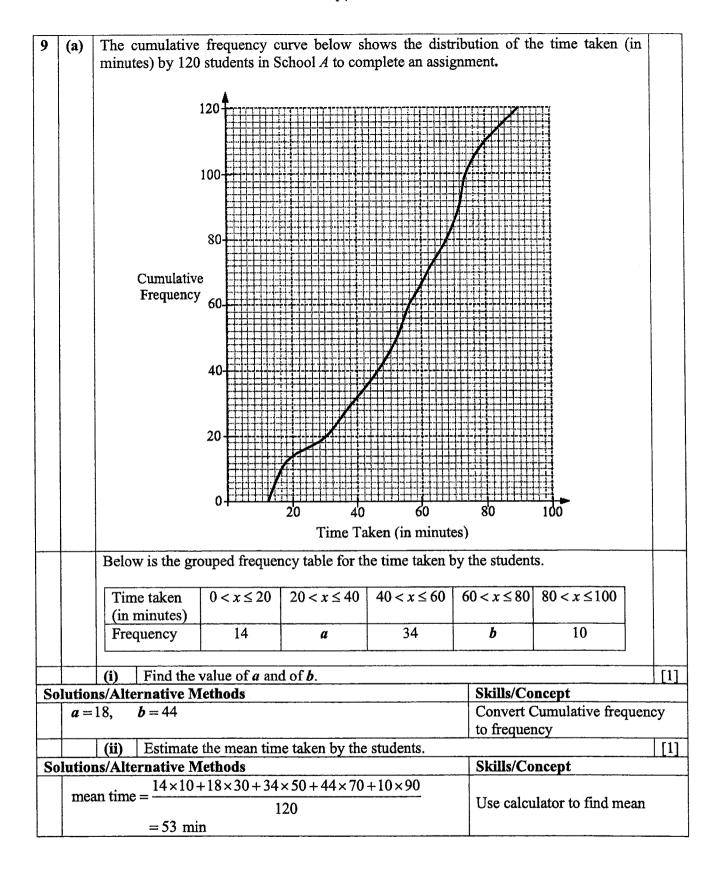
Time taken = $2 \times \frac{600}{200 - 5.55113} - \frac{10}{60}$ = $6.0046$	
= 6 hours	
Solutions/Alternative Methods	
Time taken = $\frac{600}{}$ + $\frac{600}{}$	
$\frac{11116 \text{ taken}}{200-5.55113} = \frac{200+5.55113}{200+5.55113}$	
= 6.0046	
= 6 hours	



	(d) Show that $QR$ is parallel to $ST$ , hence find the area of $\Delta PVT$ if area of triangle $\Delta PQR = 22.7 \text{ cm}^2$ .							
Sol	⊥utions	/Alternative Methods	Skills/Concept	L				
		$\Delta PQR$ is congruent to $\Delta STP$ ,						
	∠PQ	$R = \angle STP$ (corresponding $\angle$ s of congruent triangles)	Use of congruent rule					
	Вусо	$=80^{\circ}$ enverse of corresponding angles, $QR$ is parallel to $ST$ .	Corr. angles, parallel lines					
	OR							
	∠SRQ ∠TSI	$R = 40^{\circ}$ $Q = 60^{\circ} + 80^{\circ} = 140^{\circ}$ $R + \angle SRQ = 40^{\circ} + 140^{\circ} = 180^{\circ}$ . By converse of interior s, $QR$ is parallel to $ST$ .						
	OR							
	∠SVI	$Q = 180^{\circ} - 40^{\circ} - 60^{\circ} = 80^{\circ}$ (angle sum in a triangle) $R = \angle VRQ = 80^{\circ}$ . By converse of alternate angles, $QR$ allel to $ST$ .						
		V is similar to ΔPQR of ΔPTV = $\left(\frac{4}{11.52}\right)^2 \times 22.7$	Areas of similar triangles					
		= $2.7368 \text{ cm}^2$ = $2.74 \text{ cm}^2$						

A roof in the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of a triangular right prism is confidence of the shape of t	
(a) the area of triangle ABE,	[2]
Solutions/Alternative Methods	Skills/Concept
area of triangle $ABE = \frac{1}{2} \times 12 \times 12 \times \sin 120$ = 62.354 = 62.4 m <sup>2</sup>	Area of triangle involving sine
(b) $AB^2$ ,	[2]
Solutions/Alternative Methods	Skills/Concept
$AB^{2} = 12^{2} + 12^{2} - 2(12)(12)\cos 120$ $= 432$	Cosine rule
(c) AC,	[2]
Solutions/Alternative Methods	Skills/Concept
$AC = \sqrt{432 + 12^2}$ (Pythagoras' Theorem) = 24 m	Pythagoras' Theorem
(d) ∠AEC,	[3]
Solutions/Alternative Methods	Skills/Concept
$EC = \sqrt{12^2 + 12^2} \text{ (Pythagoras' Theorem)}$ $= \sqrt{288} \text{ m}$ $12^2 + \left(\sqrt{288}\right)^2 - 24^2$	Pythagoras' Theorem
$\cos \angle AEC = \frac{12^2 + \left(\sqrt{288}\right)^2 - 24^2}{2(12)(\sqrt{288})}$ $= \frac{-144}{407.293506}$ $\angle AEC = 110.7048$	Cosine rule
=110.7 (1 d.p.)	

(e)	the largest angle of elevation of $M$ viewed from a po-	int along <i>CD</i> .	[3]
Solution	s/Alternative Methods	Skills/Concept	
be Q AM	the point directly below $M$ at $AB$ be $P$ and let the point on $CD$ .  = 6 m  (M. $AB$ ) (here angle of isosceles triangle)		
PM PO:	M = 30° (base angle of isocesles triangle) = 6sin 30° = 3 m = 12 m	Sine Trigo Ratio	
tan ∠PÇ	$\angle PQM = \frac{3}{12}$ $QM = \tan^{-1} \left(\frac{1}{4}\right)$ = 14.036 = 14.0 (1 d.p.)	Tangent Trigo Ratio	



(iii)	Estimate the standard deviation of the time taken by	the students.							
	ernative Methods	Skills/Concept							
	$\frac{120^{2} + 18 \times 30^{2} + 34 \times 50^{2} + 44 \times 70^{2} + 10 \times 90^{2}}{120} - 53^{2}$	Use calculator to find S.D							
	$\frac{9200}{20} - 2809$								
1 1 '	52289								
1 1	min (3 s.f.)								
(iv)									
	Mean time taken60Standard deviation13.6								
	Make two comments comparing the time taken by t	he students from the 2 schools. [2]							
Solutions/Alt	ernative Methods	Skills/Concept							
On average same assi minutes 1	ge, students from school $B$ took longer to complete the gnment as their mean time taken of 60 minutes is 7 onger than the mean time taken of 53 minutes by rom school $A$ .	Comparing of data in context using mean by stating the difference							
students for School B minutes h	In do f the time taken to complete the assignment for from school $A$ is wider compared to students from as their standard deviation of 22.8 minutes is 9.2 igher than School $B$ 's 13.6 minutes. The time taken dents from School $B$ is more homogeneous.	Comparing of data in context using S.D. by stating the difference							
	Bryan and Chandra took part in a game of dart throwing and Chandra will hit the target in a single throw are	l l							
(i)	For the first game, all three of them throw the dart Find the probability that all of them hit the target.	[2]							
Solutions/Alt	ernative Methods	Skills/Concept							
P(all of th	nem missed) = $\frac{1}{6} \times \frac{1}{5} \times \frac{1}{4}$ = $\frac{1}{120}$	Probability of independent events							
(ii)	In the second game, they each make a single throw order of Ali, Bryan and Chandra. For this game, or will end. Find the probability the target is hit.								
Solutions/Alt	ernative Methods	Skills/Concept							
	target) = $\frac{1}{6} + \left(\frac{5}{6} \times \frac{1}{5}\right) + \left(\frac{5}{6} \times \frac{4}{5} \times \frac{1}{4}\right)$	Probability of independent events & mutually exclusive events							
	$=\frac{1}{2}$								

				full capacity of 120 sea The detail of the surve		conducted a survey to find ou ow:	t	
			-					
			Price of one ticket \$6.00	Number of people w	120	attend the concert		
			\$7.50		110			
			\$9.00		100			
			\$10.50		90			
	(a)	Write	e down the revenue he	e will get if all 120 seat	s are so	ld.	<u>Γ11</u>	
Solut			native Methods	- Will Box 11 001 120 000		Skills/Concept		
			=120×6					
		=	= \$720					
	(b)		I noticed that for eve le who attend the con		e price	of one ticket, the number of	f	
	-	(i)		ne makes three \$1.50 is	ncreases	to the price from \$6.	[1]	
Solut	ions	/Alter	native Methods			Skills/Concept		
	Pric	e after	= 6.00 + 30	1.50)				
			= \$10.50					
				10.50, 90 people will at	tend			
	Reve		= 90×10.50					
			= \$945					
		(ii)				of the tickets, explain why the		
	•	/ A T/	L.,	s is given by $720+120$	$n-15n^2$		[3]	
Solut			mative Methods $= 1.50n + 6$			Skills/Concept Find amount increase		
						The drop in number who at	tend	
			f people who will atte		Form expression for revenue			
	Reve		= (1.50n + 6)(120 - 10)	•		1 01111 0xprossion for 10 vond		
			$= 180n - 15n^2 + 720 -$					
			$= 720 + 120n - 15n^2$			1 111 1 1 10	T 54.7	
				mber of \$1.50 increase	in price	should be less than 12.	[1]	
Solu			rnative Methods			Skills/Concept		
		n > 1	•	4: 100 10 .0				
			f people who will attended for the following from t					
	w				20 orid 6	ppposite, work out how much		
		(iv)		the graph for $n < 12$ on the his ticket to maximum			[4]	
Solu	tions	/Alter	native Methods	Instruct to maximum		Concept	11-1	
Boild				ole of values & scales		ent points (at least 6) to dray	 V а	
	-	•	not given in the que			h curve		
		J			Smoot	h curve passing through all p	oints	
	Fron	n the į	graph, since revenue	is maximum at $n = 4$ ,	Know	max revenue is at $n = 4$		
	Hes	hould	charge = $4(1.50) + 6$	=\$12			···	

n	0	1	2	3	4	5	6	7	8	9	10	11
R	720	825	900	945	960	945	900	825	720	585	420	225

